



Figure 1: Streaming driven by a vibrating cylinder (left) and vibrating sharp edge (right).

GFD Project: Acoustic Streaming meets GFD

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Acoustic streaming is a technologically important wave-driven mean flow phenomenon. Viscous effects play a crucial role in classical forms of acoustic streaming, with streaming speeds being small compared to the oscillatory velocities directly induced by the sound waves.

The Effect of Baroclinicity

A novel form of *strong* acoustic streaming recently has been identified [1] in which streaming speeds are comparable to oscillatory particle velocities. The enhanced streaming speeds arise because wave (fluctuating) vorticity is produced *baroclinically* throughout the physical domain in the presence of an imposed background temperature/density gradient. Our theoretical investigations of baroclinic acoustic streaming in internal (channel) geometries demonstrate that, unlike classical Rayleigh streaming, there is fully two-way coupling between the sound waves and time-mean flow [2,3]. The aim of this GFD project is to re-examine (using asymptotic analysis and numerical simulation) a related problem: streaming-enhanced heat transfer from an oscillating hot sphere to a cooler ambient gas. Crucially, *all* prior analyses [e.g. 4] of this canonical problem tacitly but incorrectly presume that the heat transfer can be computed by treating the mean temperature as a passive scalar field advected by a pre-computed classical viscous (Rayleigh) streaming flow.

The Effect of Surface Roughness

In Rayleigh streaming, wave vorticity is generated in oscillatory Stokes boundary layers adjacent to solid surfaces. Interestingly, recent studies [5] have demonstrated the possibility for anomalously large streaming speeds emanating from a *sharp edge*. To date, however, there has only been a single compelling theoretical investigation of this “sharp-edge Rayleigh streaming” [6]. Accordingly, the aim of this GFD project is to further develop the theory, expose the underlying physical mechanisms and devise efficient numerical algorithms for simulating this novel phenomenon.

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